

TRIGONOMETRIE

$\sin(\alpha) = \frac{\text{Gegenkathete}}{\text{Hypotenuse}}$	$\tan(\alpha) = \frac{\sin(\alpha)}{\cos(\alpha)}$	Sinussatz: $\frac{a}{b} = \frac{\sin(\alpha)}{\sin(\beta)}$
$\cos(\alpha) = \frac{\text{Ankathete}}{\text{Hypotenuse}}$	$\sin^2(\alpha) + \cos^2(\alpha) = 1$	Kosinussatz: $a^2 = b^2 + c^2 - 2bc * \cos(\alpha)$
$\tan(\alpha) = \frac{\text{Gegenkathete}}{\text{Ankathete}}$	$\sin(90^\circ - \alpha) = \cos(\alpha)$	

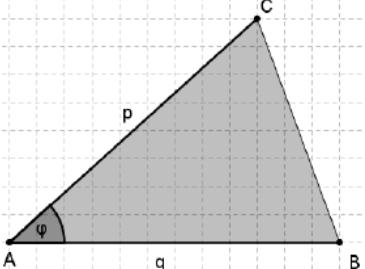
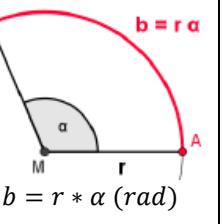
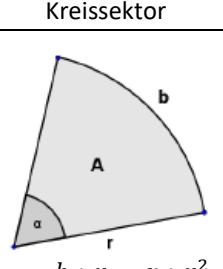
1.1 Spezielle Winkel

Dreiecke

	0°	30°	45°	60°	90°		
\sin	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1		
\cos	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0		
\tan	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	$\text{undef}\left(\frac{1}{0}\right)$	$s = 1$	$h = \sqrt{3}$

1.2 Flächeninhalt

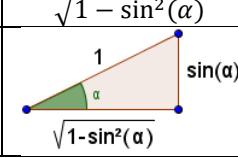
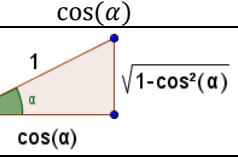
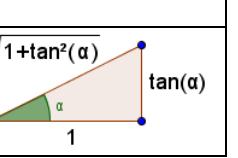
Bogen

 $A = \frac{1}{2} * p * q * \sin(\varphi)$	Bogenmass	Bogenlänge	Kreissektor
	$180^\circ = \pi$	$b = r * \alpha \text{ (rad)}$	$A = \frac{b * r}{2} = \frac{\alpha * r^2}{2}$
	$\alpha(\text{bog}) = \frac{\pi}{180^\circ} * \alpha(\text{grad})$ $\alpha(\text{grad}) = \frac{180^\circ}{\pi} * \alpha(\text{bog})$		

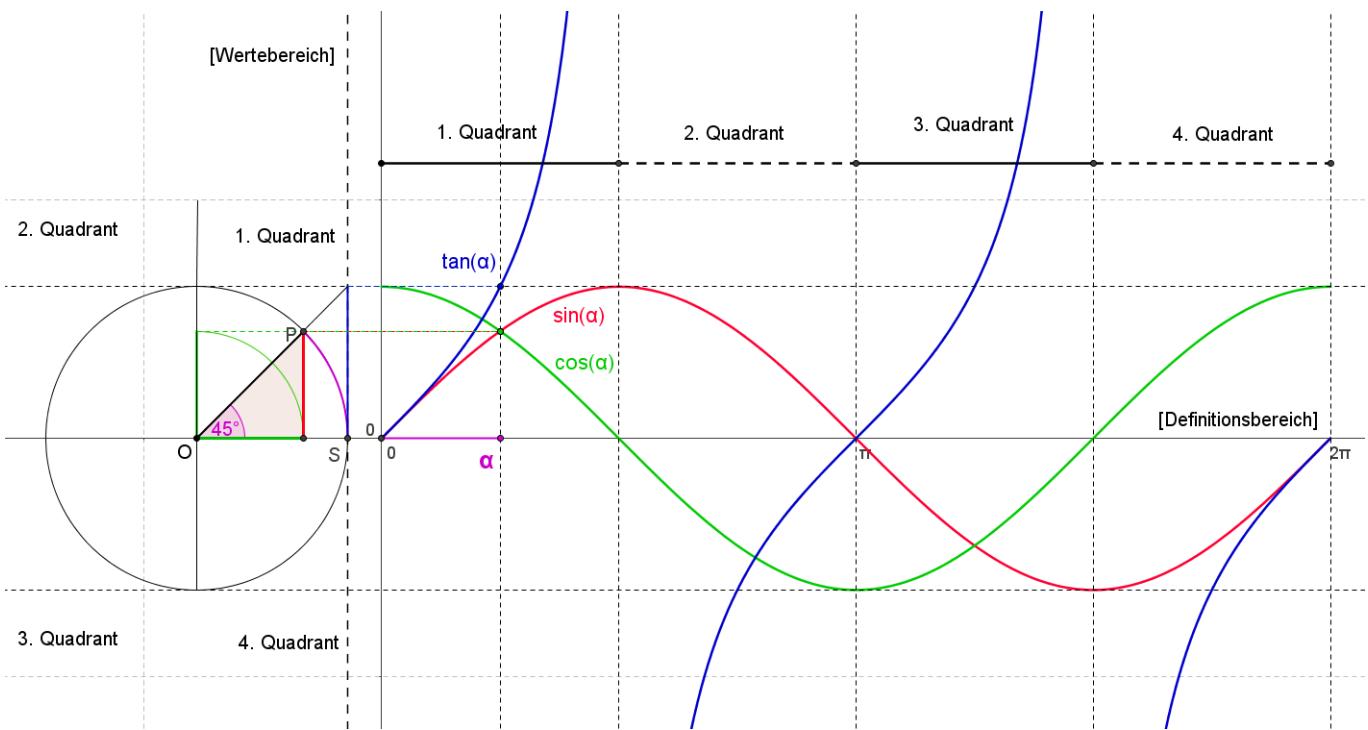
1.3 Definition

Funktion	Definition	Definitionsbereich	Wertebereich	Symmetrie
$\sin(\alpha)$	y-Koordinate des Punktes P auf dem Einheitskreis	$D = R$	$W = [-1; 1]$	$\sin(-x) = -\sin(x)$
$\cos(\alpha)$	x-Koordinate des Punktes P auf dem Einheitskreis	$D = R$	$W = [-1; 1]$	$\cos(-x) = \cos(x)$
$\tan(\alpha)$	y-Koordinate des Punktes H auf dem Tangententräger	$D = R \setminus \left\{ \frac{\pi}{2} + k * \pi \mid k \in \mathbb{Z} \right\}$	$W = R$	$\tan(-x) = -\tan(x)$

1.4 Ersetzungen

	<i>sinus</i>	<i>cosinus</i>	<i>tangens</i>
$\sin(\alpha)$	—	$\sqrt{1 - \cos^2(\alpha)}$	$\frac{\tan(\alpha)}{\sqrt{1 + \tan^2(\alpha)}}$
$\cos(\alpha)$	$\sqrt{1 - \sin^2(\alpha)}$	—	$\frac{1}{\sqrt{1 + \tan^2(\alpha)}}$
$\tan(\alpha)$	$\frac{\sin(\alpha)}{\sqrt{1 - \sin^2(\alpha)}}$	$\frac{\sqrt{1 - \cos^2(\alpha)}}{\cos(\alpha)}$	—
			

1.5 Einheitskreis und Funktionsgraph



1.6 Umkehrfunktionen

